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**DEPARTMENT OF AEROSPACE AND MECHANICAL ENGINEERING**

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Introduction to Acoustics

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**Homework 7**

- I. Consider a narrow tube extending from  $x = 0$  to  $x = L$  with both ends open, i.e., the boundary condition at each end is  $p = 0$ . Find the natural frequencies and the eigenfunctions describing the acoustic pressure in the tube.
- II. A piston at the  $x = 0$  end of a tube of length  $L$  and radius  $a$  is oscillating with the velocity

$$v = \hat{v}e^{i(kx - \omega t)}. \quad (1)$$

1. The specific acoustic impedance at the end  $x = L$  is  $\epsilon\rho c$ , where  $\epsilon$  is a small positive real number, i.e.,  $\epsilon \ll 1$ . Give the approximate expression for the lowest resonance frequency and the peak average acoustic power output of the piston for frequencies in the vicinity of this resonance.
2. For a flanged duct at low frequency,  $\lambda \gg a$ , the specific acoustic impedance at the end  $x = L$  is given by

$$Z_L = \rho_0 c_0 \left[ \frac{1}{2}(ka)^2 - i \frac{8}{3\pi} ka \right]. \quad (2)$$

Calculate the resonance frequencies and efficient length  $L_{eff}$  defined as the tube length if the  $Z_L = 0$ . Calculate the power radiated from the duct. Take a typical example of your choice to calculate the relevant quantities.

3. For an unflanged open duct at low frequency,  $\lambda \gg a$ , the specific acoustic impedance at the end  $x = L$  is given by

$$Z_L = \rho_0 c_0 \left[ \frac{1}{4}(ka)^2 - i0.6ka \right]. \quad (3)$$

Calculate the resonance frequencies and efficient length  $L_{eff}$  defined as the tube length if the  $Z_L = 0$ . Calculate the power radiated from the duct. Take a typical example of your choice to calculate the relevant quantities.